

Introduction to CS 293S
Advanced Compiler Technology
--- Code Optimizations for Scalar and
Parallel Programs

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Review of Last Lecture

- Course overview
- Code optimization
 - Metric & importance of program quality
 - Who makes the enhancement?
 - Compiler is the primary engine
 - How to do it?
 - Program analysis
 - Program transformations
- Consideration of optimization
- Sources of inefficiency

This Lecture

- Redundancy Elimination

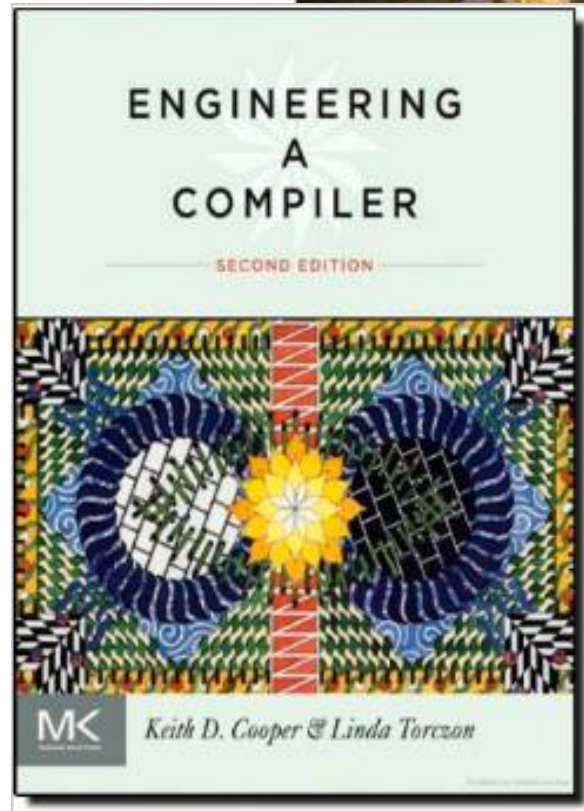
Topics

- Types of intermediate representations of a program
- Removing redundant expressions
 - DAG: version tracking
 - Linear representation: value numbering

Reference books



CT book



Intermediate Representations

(Details in Ch. 5 of CT book)

Why use an intermediate representation?

Key insight: An intermediate representation is a compile-time data structure

- break the compiler into manageable pieces – good software engineering technique
- simplifies handling of “poly-architecture” problem
m languages, n targets \Rightarrow m+n components

Intermediate Representations

(Details in Ch. 5 of CT book)

What are the good properties of an intermediate representation?

- ease of generation
- ease of manipulation
- cost of manipulation
- level of abstraction
- freedom of expression
- size of typical procedure

Level of exposed detail is a crucial consideration. The selection of IR would affect the speed and effectiveness of the compiler.

Types of Intermediate Representations

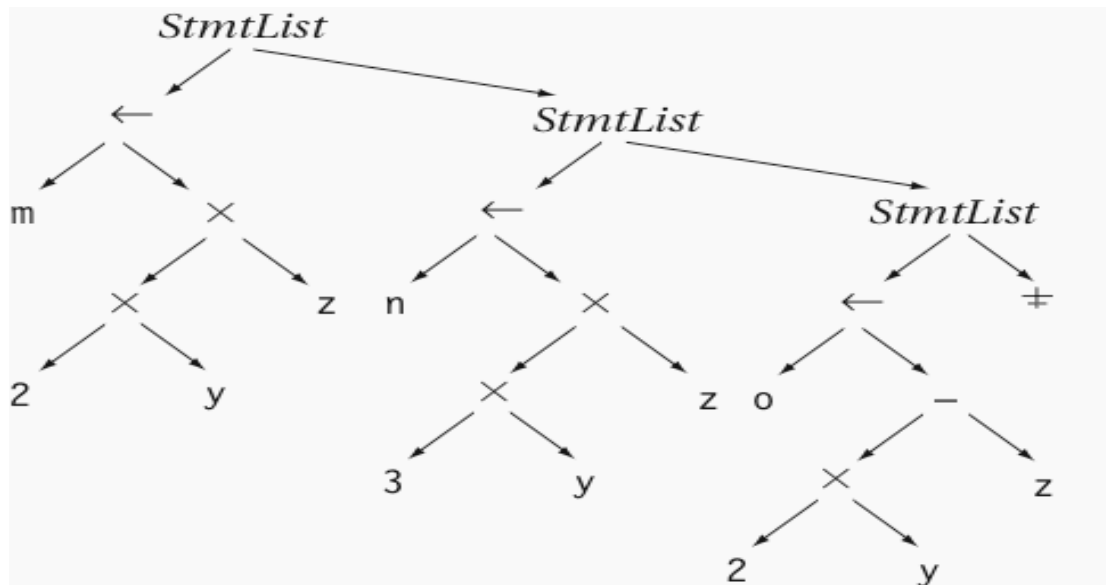
(Details in Ch. 5 of CT book)

Three major categories

- I: Structural
 - Graphically oriented
 - Heavily used in source-to-source translators
 - Tend to be large

Examples:

Trees,
Directed Acyclic Graphs (DAGs),
Dependence graph



m \leftarrow 2 x y x z
 n \leftarrow 3 x y x z
 o \leftarrow 2 x y - z

Types of Intermediate Representations

(Details in Ch. 5 of CT book)

Three major categories

- 2: Linear
 - Pseudo-code for an abstract machine
 - Simple, compact data structures
 - Easier to rearrange

Examples:
Three-address code
 $X \leftarrow y \text{ op } z$

$z \leftarrow x - 2 * y$

becomes

$t \leftarrow 2 * y$
 $z \leftarrow x - t$

Types of Intermediate Representations

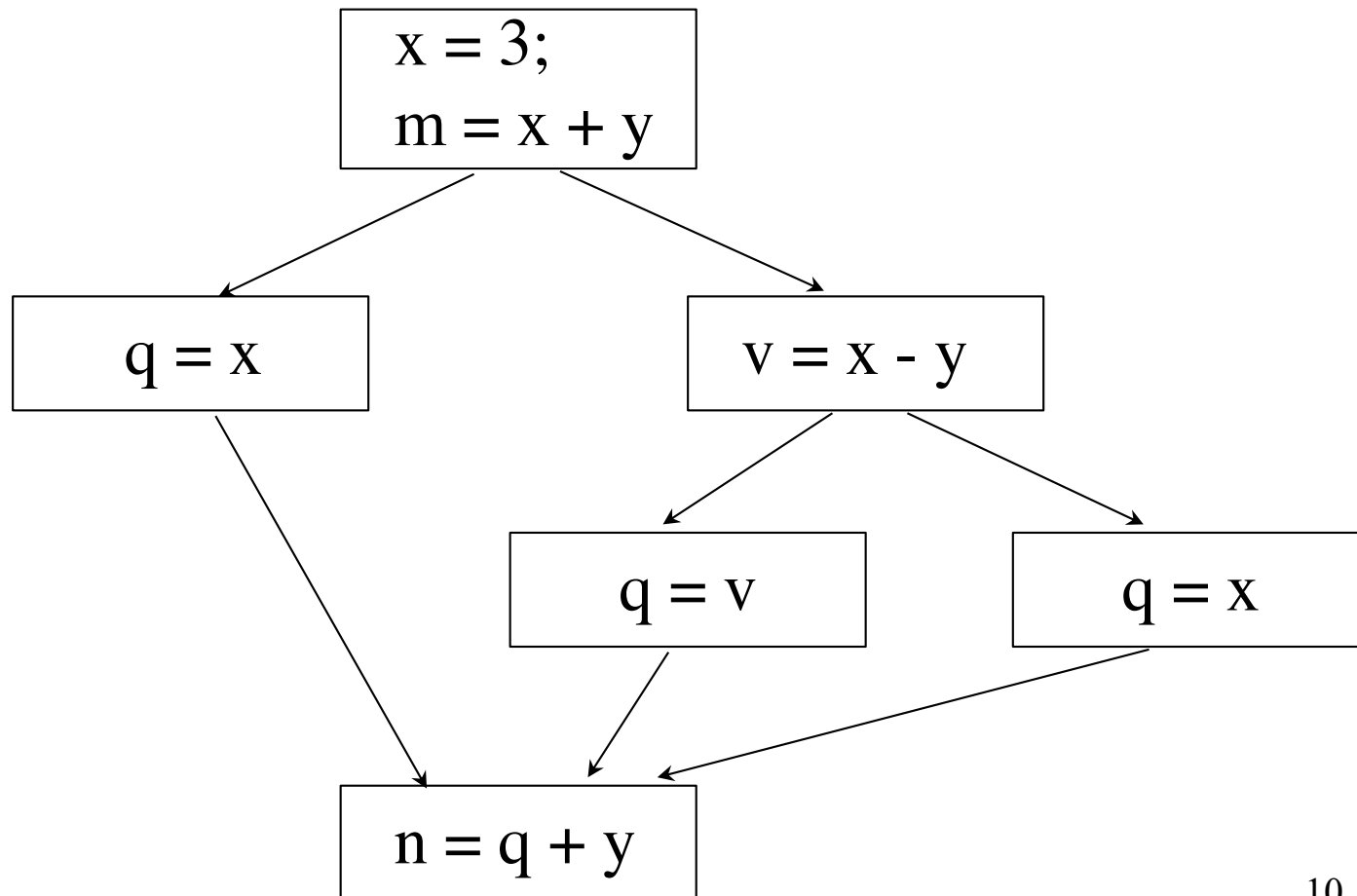
(Details in Ch. 5 of CT book)

Three major categories

□ 3: Hybrid

□ Combination of graphs and linear code

Example:
Control-flow graph



Redundancy Removal: A Deep Look

Redundancy Removal

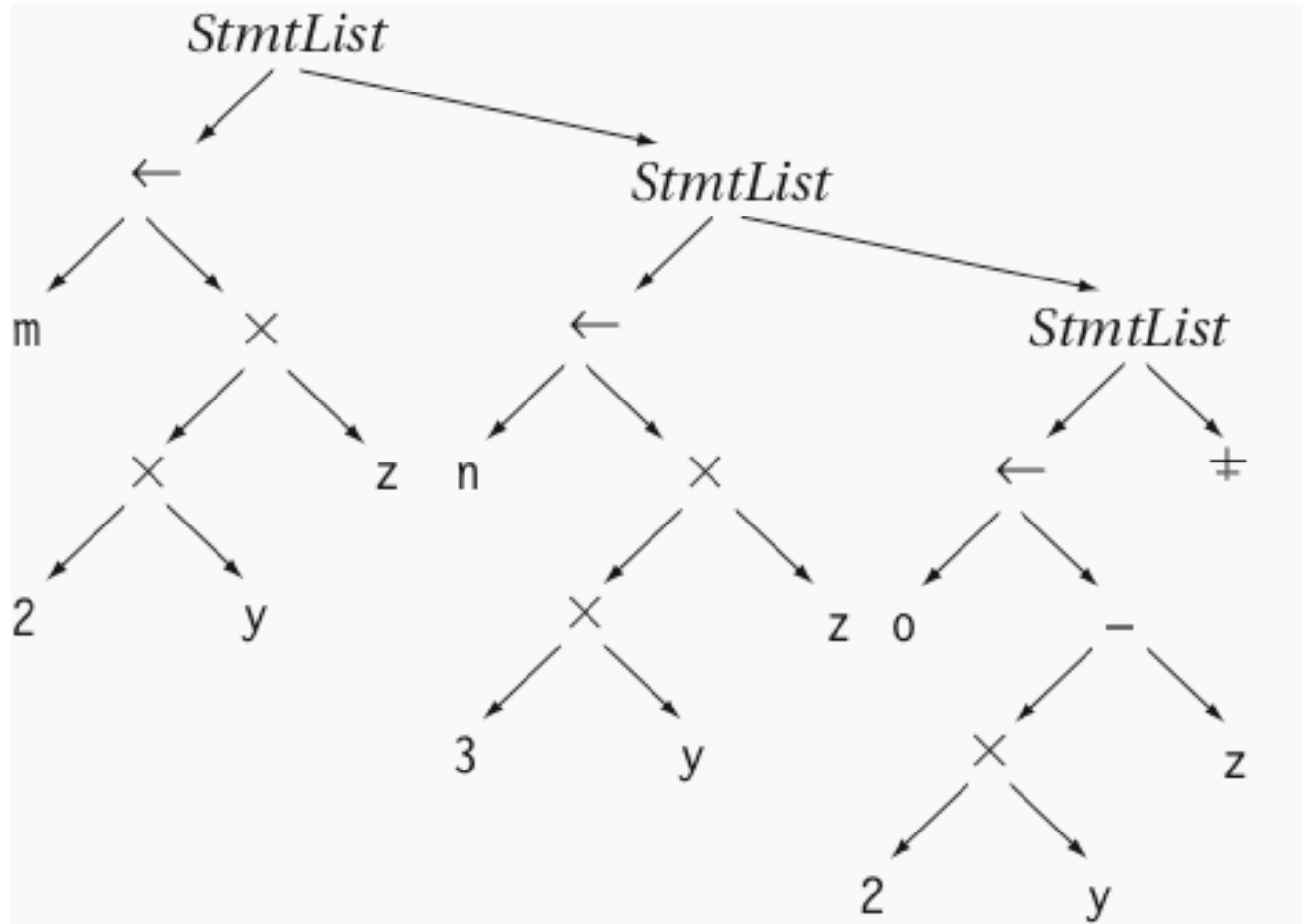
- Replace redundant expressions by their values
- Example

```
m  $\leftarrow$  2 x y x z  
n  $\leftarrow$  3 x y x z  
o  $\leftarrow$  2 x y - z
```

```
t  $\leftarrow$  2 x y  
m  $\leftarrow$  t x z  
  
n  $\leftarrow$  3 x y x z  
  
o  $\leftarrow$  t - z
```

Method 1: Finding Redundancy in Directed Acyclic Graph (DAG)

$m \leftarrow 2 \times y \times z$
 $n \leftarrow 3 \times y \times z$
 $o \leftarrow 2 \times y - z$



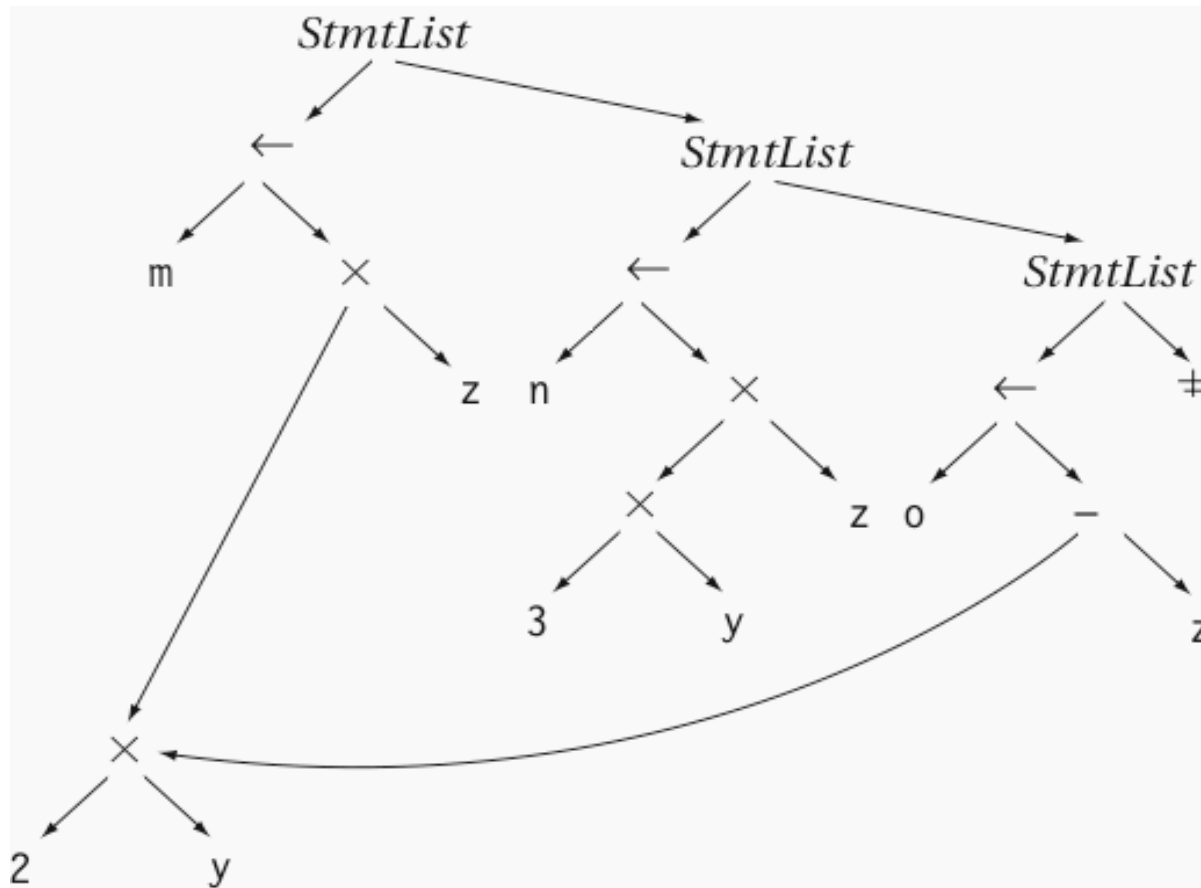
A directed acyclic graph (DAG) is an AST with a unique node for each value.

DAG: Eliminating Identical Subtrees

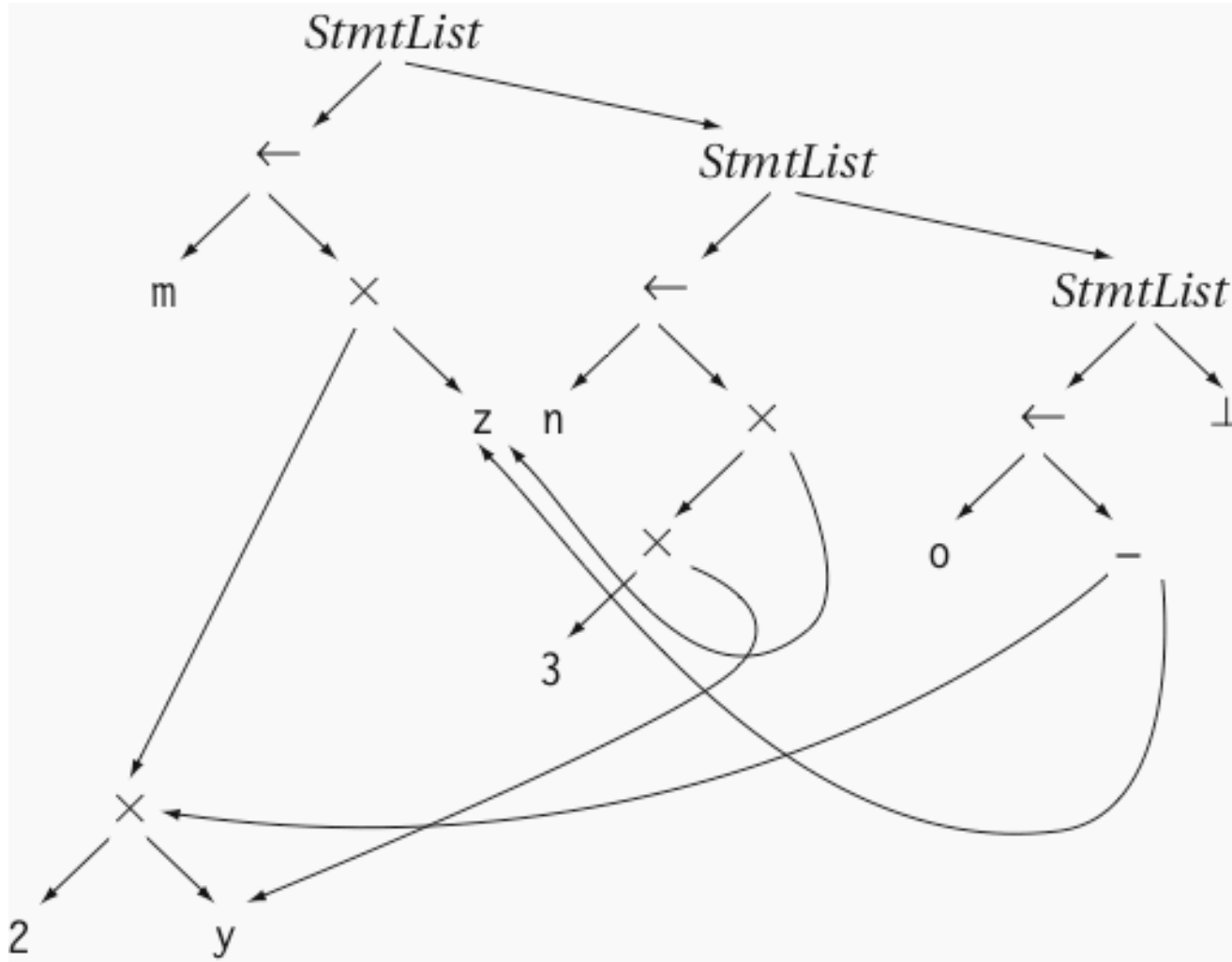
$m \leftarrow \underline{2} \times y \times z$
 $n \leftarrow 3 \times y \times z$
 $o \leftarrow \underline{2} \times y - z$

Using hash-based constructor:

- **key** is the textual notion of operators and operands;
- **value** is the node number or address.



Finding Redundancy in DAG



$m \leftarrow \underline{2} \ x \ y \ x \ z$
 $n \leftarrow 3 \ x \ y \ x \ z$
 $o \leftarrow \underline{2} \ x \ y \ - \ z$

Using hash-based constructor:

- **key** is the textual notion of operators and operands;
- **value** is the node number or address.

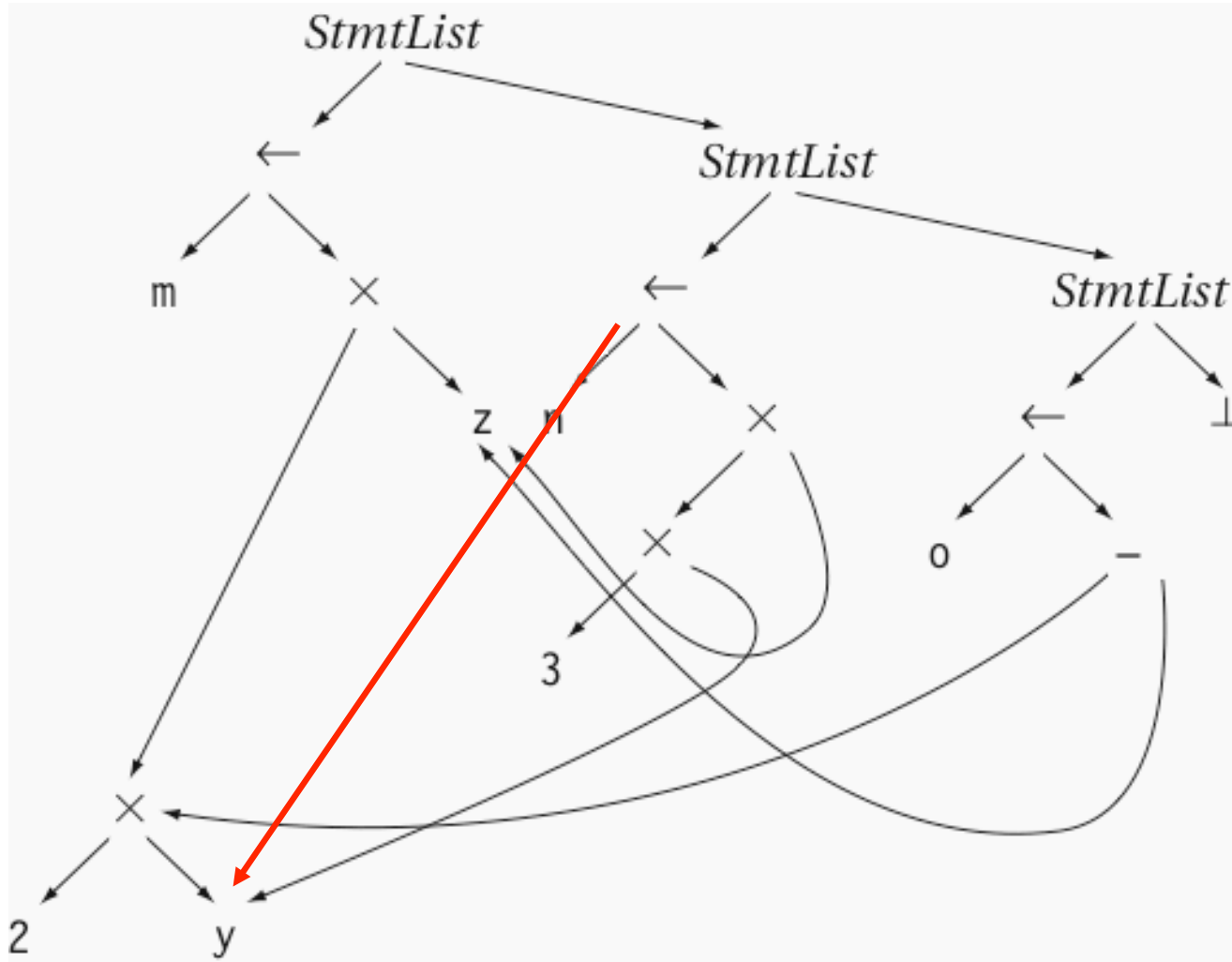
Limitations of the method?

Original Code
m \leftarrow 2 x y x z
y \leftarrow 3 x y x z
o \leftarrow 2 x y - z

Using hash-based constructor:

- **key** is the textual notion of operators and operands;
- **value** is the node number or address.

Problem



```
m <-- 2 x y x z
y <-- 3 x y x z
o <-- 2 x y - z
```



~~```
t <-- 2 x y
m <-- t x z
y <-- 3 x y x z
o <-- t - z
```~~

# *Version Tracking*

```
m <-- 2 x y x z
y <-- 3 x y x z
o <-- 2 x y - z
```

Associate a counter with each variable for version tracking

```
m1 <-- 2 x y1 x z1
y2 <-- 3 x y1 x z1
o1 <-- 2 x y2 - z1
```

*Missing Any Opportunities?*

## *Missing Any Opportunities?*

### Original Code

$a \leftarrow x + y$

$z \leftarrow y$

$d \leftarrow 17$

$c \leftarrow x + z$

- Is there any redundant expression?
- Can the DAG-based approach recognize it?

The hash-based constructor uses a textual notion of "equality",

- so  $y$  equals  $y$ , independent of its value.
- $z$  does not equal  $y$ , independent of its value.

# *Value Numbering*

- An old idea: Balke 1968 or Ershov 1954
  - Value instead of textual notation
- This technique was invented for low-level, linear IRs
- Equivalent methods exist for trees (build a DAG )

# *Linear Representation:*

Linear IR Example: Three Address Code

□ Statement form:

$$x \leftarrow y \text{ op } z$$

With 1 operator (op) and, at most, 3 names (x, y, z)

Example:

$$z \leftarrow x - 2 * y$$

becomes

$$\begin{array}{l} t \leftarrow 2 * y \\ z \leftarrow x - t \end{array}$$

**Statements are executed sequentially.**

# Local Value Numbering

## Basic Algorithm

For each expression  $e$

(assuming in the form  $\text{result}_e \leftarrow o_1 \text{ op } o_2$ )

□ Get value numbers for operands from hash lookup table, represented by  $\text{VN}(o_1)$ ,  $\text{VN}(o_2)$ . If no such key exists, insert these keys to the hash table with new value numbers;

□ Search with hash key  $\langle \text{op}, \text{VN}(o_1), \text{VN}(o_2) \rangle$ ,

If no such key exists,

1. insert the key to the hash table with a new value number;
2. use the same value number for  $\text{result}_e$  and insert them to hash table.

else,

get the value of this key, use the same value number for  $\text{result}_e$ , and insert them to hash table.

# Local Value Numbering to Find Redundancy

## An example

### Original Code

$a \leftarrow x + y$

$z \leftarrow y$

$d \leftarrow 17$

$c \leftarrow x + z$

### With VNs

$a^3 \leftarrow x^1 + y^2$

$z^2 \leftarrow y^2$

$d^4 \leftarrow 17$

$c^3 \leftarrow x^1 + z^2$

### Hash Table for VN

$\{ \langle x, 1 \rangle, \langle y, 2 \rangle, \langle \langle +, 1, 2 \rangle, 3 \rangle, \langle a, 3 \rangle \}$

$\{ \dots, \langle z, 2 \rangle \}$

$\{ \dots, \langle z, 2 \rangle, \langle 17, 4 \rangle, \langle d, 4 \rangle \}$

$\{ \dots, \langle z, 2 \rangle, \langle 17, 4 \rangle, \langle d, 4 \rangle, \langle c, 3 \rangle \}$

Compare Value Num with Version Num. (The way they get increase; why the latter is insufficient for the example.)



# Rewritten for Redundancy Elimination

## An example

### Original Code

$a \leftarrow x + y$   
 $z \leftarrow y$   
 $d \leftarrow 17$   
 $c \leftarrow x + z$

### With VNs

$a^3 \leftarrow x^1 + y^2$   
 $z^2 \leftarrow y^2$   
 $d^4 \leftarrow 17$   
 $c^3 \leftarrow x^1 + z^2$

### Hash Table for VN

$\{ \langle x, 1 \rangle, \langle y, 2 \rangle, \langle \langle +, 1, 2 \rangle, 3 \rangle, \langle a, 3 \rangle \}$   
 $\{ \dots, \langle z, 2 \rangle \}$   
 $\{ \dots, \langle z, 2 \rangle, \langle 17, 4 \rangle, \langle d, 4 \rangle \}$   
 $\{ \dots, \langle z, 2 \rangle, \langle 17, 4 \rangle, \langle d, 4 \rangle, \langle c, 3 \rangle \}$

### Rewritten

$a \leftarrow x + y$   
 $z \leftarrow y$   
 $d \leftarrow 17$   
 $c \leftarrow a$

### Hash Table for Rewritten

$\{ \langle 1, x \rangle, \langle 2, y \rangle, \langle 3, a \rangle \}$   
 $\{ \langle 1, x \rangle, \langle 2, y \rangle, \langle 3, a \rangle \}$   
 $\{ \langle 1, x \rangle, \langle 2, y \rangle, \langle 3, a \rangle, \langle 4, 17 \rangle \}$   
 $\{ \langle 1, x \rangle, \langle 2, y \rangle, \langle 3, a \rangle, \langle 4, 17 \rangle \}$

# Resolving Overwritten Issue

## An example

### Original Code

$a \leftarrow x + y$   
 $z \leftarrow y$   
\*  $b \leftarrow x + y$   
 $a \leftarrow 17$   
\*  $c \leftarrow x + y$

Two redundancies  
marked by \*

### With VNs

$a^3 \leftarrow x^1 + y^2$   
 $z^2 \leftarrow y^2$   
\*  $b^3 \leftarrow x^1 + y^2$   
 $a^4 \leftarrow 17$   
\*  $c^3 \leftarrow x^1 + y^2$

### Rewritten

$a \leftarrow x + y$   
 $z \leftarrow y$   
\*  $b \leftarrow a$   
 ~~$a \leftarrow 17$~~   
\*  ~~$c \leftarrow a$~~

### Hash Table for Rewritten

{<1,x>, <2,y>, <3,a>}

{<1,x>, <2,y>, <3,a>}

{<1,x>, <2,y>, <3,a>, <4,17>}

{<1,x>, <2,y>, <3,a>, <4,17>}

### Optional Solutions:

- Use  $c^3 \leftarrow b^3$
- Save  $a^3$  in  $t^3$
- **Rename around it (best)**

# Renaming in Value Numbering

## Example (continued)

### Original Code

$a_0 \leftarrow x_0 + y_0$   
 $z_0 \leftarrow y_0$   
\*  $b_0 \leftarrow x_0 + y_0$   
 $a_1 \leftarrow 17$   
\*  $c_0 \leftarrow x_0 + y_0$

### With VNs

$a_0^3 \leftarrow x_0^1 + y_0^2$   
 $z_0^2 \leftarrow y_0^2$   
\*  $b_0^3 \leftarrow x_0^1 + y_0^2$   
 $a_1^4 \leftarrow 17$   
\*  $c_0^3 \leftarrow x_0^1 + y_0^2$

### Rewritten

$a_0 \leftarrow x_0 + y_0$   
 $z_0 \leftarrow y_0$   
\*  $b_0 \leftarrow a_0$   
 $a_1 \leftarrow 17$   
\*  $c_0 \leftarrow a_0$

### Hash Table for Rewritten

$\{ \langle 1, x_0 \rangle, \langle 2, y_0 \rangle, \langle 3, a_0 \rangle \}$   
 $\{ \langle 1, x_0 \rangle, \langle 2, y_0 \rangle, \langle 3, a_0 \rangle \}$   
 $\{ \langle 1, x_0 \rangle, \langle 2, y_0 \rangle, \langle 3, a_0 \rangle, \langle 4, 17 \rangle \}$   
 $\{ \langle 1, x_0 \rangle, \langle 2, y_0 \rangle, \langle 3, a_0 \rangle, \langle 4, 17 \rangle \}$

### Renaming:

- Give each value a unique name

### Result:

- $a_0$  is available
- Rewriting just works

## *Reordering based on associativity*

- The order in which expressions are written matters
- Example: either  $2 \times y$  or  $y \times z$  will be missed in left- or right-associative treatment.

$$m \leftarrow 2 \times y \times z$$

$$n \leftarrow 3 \times y \times z$$

$$o \leftarrow 2 \times y - z$$

- Example:  $3 \times a \times 5$

## *A Hard Problem: Pointer Assignments*

- $*p = 17$  could force every variable in a program to increase their version number.
- A major motivation for pointer analysis

### Original Code

$a \leftarrow x + y$

$b \leftarrow w + v$

$*p \leftarrow 17$

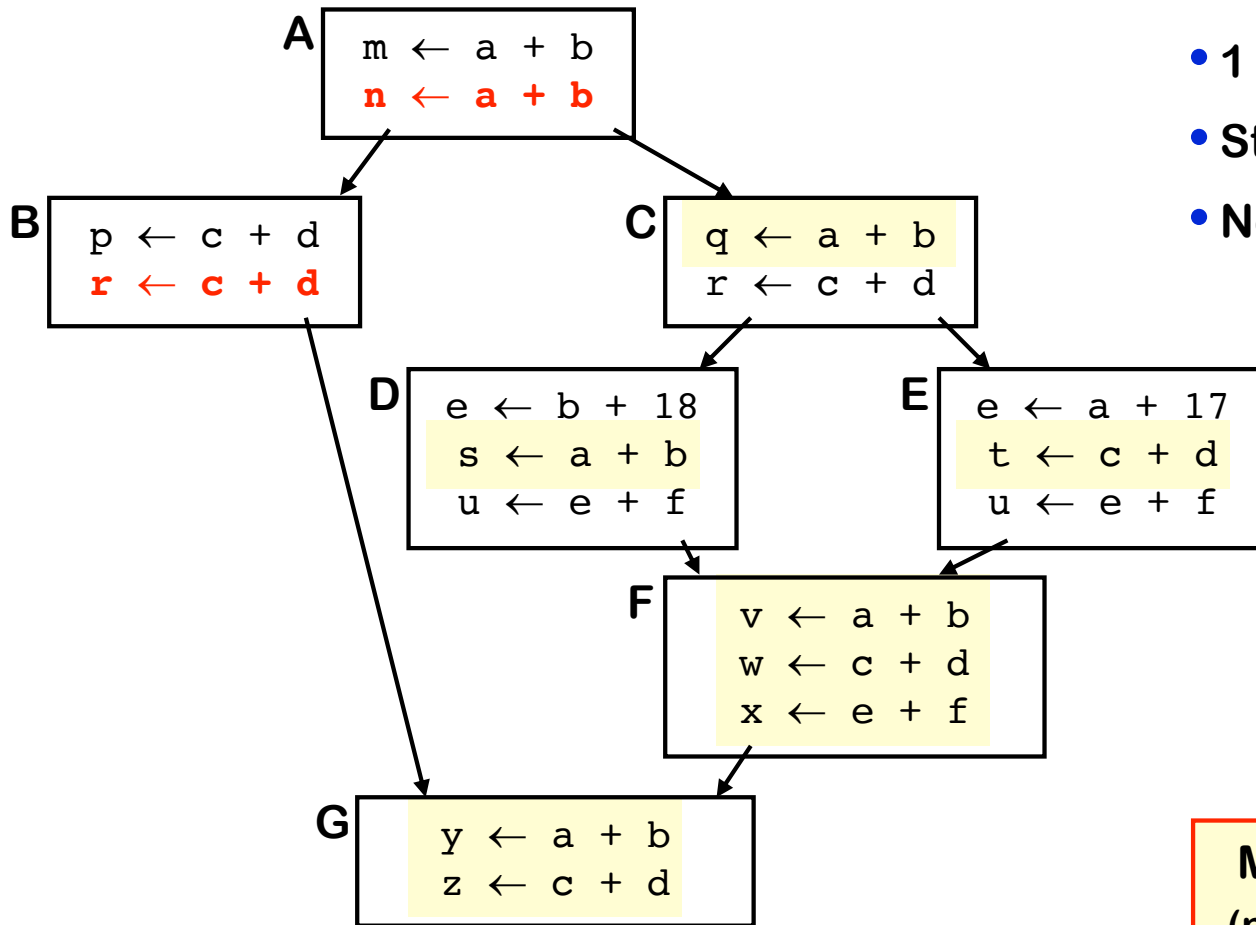
$c \leftarrow x + y$

$d \leftarrow w + v$

*So far...*

- Removing redundant expressions
  - DAG: version tracking
  - Linear representation: value numbering

# Local Value Numbering $\leftrightarrow$ Linear IR



## Local Value Numbering

- 1 block at a time
- Strong local results
- No cross-block effects

**Missed opportunities**  
(need stronger methods)